

Example 1:

a.) What is the acceleration due to gravity at the surface of Venus?

( $M_V = 4.88 \times 10^{24}$  kg and  $R_V = 6.07 \times 10^6$  m)

b.) What is the escape velocity for an object on the surface of Venus?

c.) What is the total energy of a satellite with a mass of 15,000 kg orbiting in a circular orbit 200 km above the surface of Venus?

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Example 1:  $M_V = 4.88 \times 10^{24}$  kg and  $R_V = 6.07 \times 10^6$  m

a.)  $g_V = ?$

$$F_g = G \frac{M_V m}{R_V^2} = mg_V$$

$$g_V = G \frac{M_V}{R_V^2} = \left( 6.67 \times 10^{-11} \frac{\text{N} \cdot \text{m}^2}{\text{kg}^2} \right) \frac{(4.88 \times 10^{24} \text{ kg})}{(6.07 \times 10^6 \text{ m})^2}$$

$$g_V = 8.83 \frac{\text{m}}{\text{s}^2}$$

b.)  $v_e = ?$

$$K = -U \quad \text{so} \quad \frac{1}{2} m v_e^2 = G \frac{M_V m}{R_V}$$

$$v_e = \sqrt{2G \frac{M_V}{R_V}} = \sqrt{2 \left( 6.67 \times 10^{-11} \frac{\text{N} \cdot \text{m}^2}{\text{kg}^2} \right) \frac{(4.88 \times 10^{24} \text{ kg})}{(6.07 \times 10^6 \text{ m})}}$$

$$v_e = 10,356 \frac{\text{m}}{\text{s}}$$

Example 1:

c.)  $E = ?$

$M_V = 4.88 \times 10^{24}$  kg,  $R_V = 6.07 \times 10^6$  m,  $m = 15,000$  kg, and  $d = 200$  km

$$E = K + U = \frac{1}{2} m v^2 - G \frac{M_V m}{r}$$

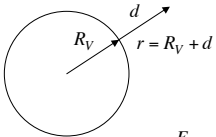
$$F_g = G \frac{M_V m}{r^2} = m a_c = m \frac{v^2}{r} \quad \text{so} \quad v = \sqrt{G \frac{M_V}{r}}$$

$$E = \frac{1}{2} m \left( \sqrt{G \frac{M_V}{r}} \right)^2 - G \frac{M_V m}{r} = \frac{1}{2} G \frac{M_V m}{r} - G \frac{M_V m}{r}$$

$$E = -\frac{1}{2} G \frac{M_V m}{r} = -\frac{1}{2} G \frac{M_V m}{R_V + d}$$

$$E = -\frac{1}{2} \left( 6.67 \times 10^{-11} \frac{\text{N} \cdot \text{m}^2}{\text{kg}^2} \right) \frac{(4.88 \times 10^{24} \text{ kg})(15,000 \text{ kg})}{(6.07 \times 10^6 \text{ m} + 2.0 \times 10^5 \text{ m})}$$

$$E = -3.9 \times 10^{11} \text{ J}$$



Example 2:

What is the weight of 85 kg person on the surface of Pluto?

( $M_P = 1.2 \times 10^{22}$  kg and  $R_P = 1.15 \times 10^6$  m)

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Example 2:  $M_P = 1.2 \times 10^{22}$  kg,  $R_P = 1.15 \times 10^6$  m, and  $m = 85$  kg

$F_g = ?$

$$F_g = G \frac{M_P m}{R_P^2}$$

$$F_g = \left( 6.67 \times 10^{-11} \frac{\text{N} \cdot \text{m}^2}{\text{kg}^2} \right) \frac{(1.2 \times 10^{22} \text{ kg})(85 \text{ kg})}{(1.15 \times 10^6 \text{ m})^2}$$

$$F_g = 51.4 \text{ N}$$

$$g_P = G \frac{M_P}{R_P^2} = \left( 6.67 \times 10^{-11} \frac{\text{N} \cdot \text{m}^2}{\text{kg}^2} \right) \frac{(1.2 \times 10^{22} \text{ kg})}{(1.15 \times 10^6 \text{ m})^2}$$

$$g_P = 0.61 \frac{\text{m}}{\text{s}^2}$$

$$F_g = m g_P = (85 \text{ kg}) \left( 0.61 \frac{\text{m}}{\text{s}^2} \right)$$

$$F_g = 51.4 \text{ N}$$

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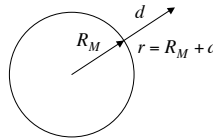
Example 3:

Find the speed of a satellite that would orbit Mars 200 km above its surface.

( $M_M = 6.42 \times 10^{23}$  kg and  $R_M = 3.38 \times 10^6$  m)

Example 3:  $M_M = 6.42 \times 10^{23}$  kg,  $R_M = 3.38 \times 10^6$  m, and  $d = 200$  km

$v = ?$



$$F_g = G \frac{M_M m}{r^2} = ma_c = m \frac{v^2}{r}$$

$$v = \sqrt{G \frac{M_M}{r}}$$

$$v = \sqrt{G \frac{M_M}{R_M + d}}$$

$$v = \sqrt{\left(6.67 \times 10^{-11} \frac{\text{N} \cdot \text{m}^2}{\text{kg}^2}\right) \frac{(6.42 \times 10^{23} \text{ kg})}{(3.38 \times 10^6 \text{ m} + 2.0 \times 10^5 \text{ m})}}$$

$$v = 3459 \frac{\text{m}}{\text{s}}$$

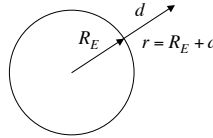
Example 4:

How many minutes would it take a satellite to orbit Earth 150 km above its surface?

( $M_E = 5.98 \times 10^{24}$  kg and  $R_E = 6.37 \times 10^6$  m)

Example 4:  $M_E = 5.98 \times 10^{24}$  kg,  $R_E = 6.37 \times 10^6$  m, and  $d = 150$  km

$T = ?$



$$F_g = G \frac{M_E m}{r^2} = ma_c = m \frac{v^2}{r}$$

$$v = \sqrt{G \frac{M_E}{r}} = \frac{2\pi r}{T}$$

$$T = 2\pi r \sqrt{\frac{r}{GM_E}} = 2\pi \sqrt{\frac{r^3}{GM_E}}$$

$$T = 2\pi \sqrt{\frac{(R_E + d)^3}{GM_E}}$$

$$T = 2\pi \sqrt{\frac{(6.37 \times 10^6 \text{ m} + 1.5 \times 10^5 \text{ m})^3}{\left(6.67 \times 10^{-11} \frac{\text{N} \cdot \text{m}^2}{\text{kg}^2}\right) (5.98 \times 10^{24} \text{ kg})}}$$

$$T = 5238 \text{ s} = 87.3 \text{ min}$$