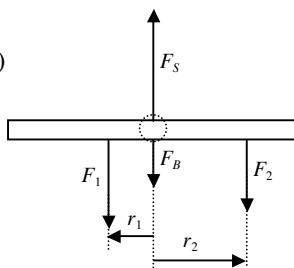
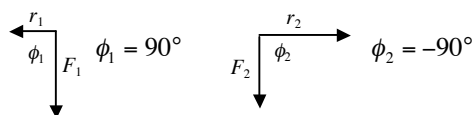


## HO 25.1 Solutions

1.)

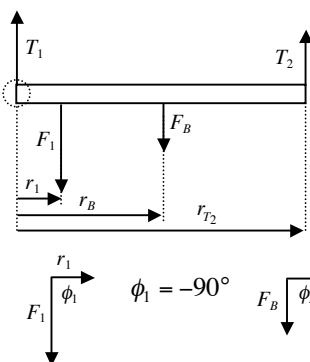


$$F_B = 40 \text{ N}, F_1 = 500 \text{ N}, \text{ and } F_2 = 350 \text{ N}$$

 using the center of the board as a reference for torque  $r_1 = 1.5 \text{ m}$  and  $r_B = r_S = 0$ 

 conditions for static equilibrium are  $\sum F_x = 0$ ,  $\sum F_y = 0$ , and  $\sum \tau = 0$ 

$$\text{if } \sum \tau = 0 \text{ then } \tau_1 + \tau_2 = 0 \text{ and } r_1 F_1 \sin \phi_1 + r_2 F_2 \sin \phi_2 = 0 \text{ so } r_2 = \frac{-r_1 F_1 \sin \phi_1}{F_2 \sin \phi_2} = \frac{-(1.5 \text{ m})(500 \text{ N}) \sin 90^\circ}{(350 \text{ N}) \sin(-90^\circ)} = \boxed{2.14 \text{ m}}$$

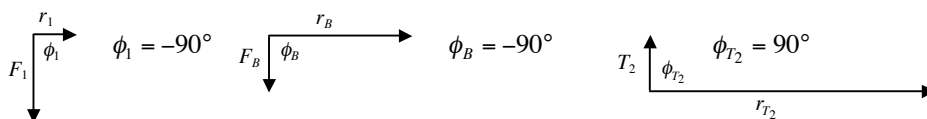
2.)



$$F_B = 100 \text{ N} \text{ and } F_1 = 400 \text{ N}$$

using the left end of the board as a reference for torque

$$r_1 = 2.0 \text{ m}, r_B = 5.0 \text{ m}, r_{T_2} = 10 \text{ m}, \text{ and } r_{T_1} = 0$$

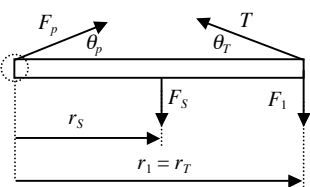

 conditions for static equilibrium are  $\sum F_x = 0$ ,  $\sum F_y = 0$ , and  $\sum \tau = 0$ 

$$\text{if } \sum \tau = 0 \text{ then } \tau_1 + \tau_B + \tau_{T_2} = 0 \text{ and } r_1 F_1 \sin \phi_1 + r_B F_B \sin \phi_B + r_{T_2} T_2 \sin \phi_{T_2} = 0 \text{ so } T_2 = \frac{-r_1 F_1 \sin \phi_1 - r_B F_B \sin \phi_B}{r_{T_2} \sin \phi_{T_2}}$$

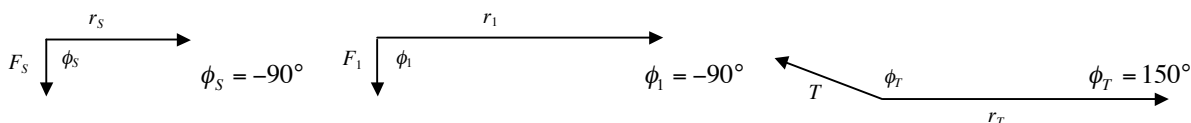
$$T_2 = \frac{-(2.0 \text{ m})(400 \text{ N}) \sin(-90^\circ) - (5.0 \text{ m})(100 \text{ N}) \sin(-90^\circ)}{(10 \text{ m}) \sin 90^\circ} = \boxed{130 \text{ N}}$$

$$\text{if } \sum F_y = 0 \text{ then } T_1 + T_2 - F_1 - F_B = 0 \text{ and } T_1 = F_1 + F_B - T_2 = 400 \text{ N} + 100 \text{ N} - 130 \text{ N} = \boxed{370 \text{ N}}$$

3.)



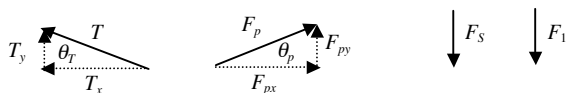
$$F_S = 100 \text{ N}, F_1 = 100 \text{ N}, \theta_T = 30^\circ, \text{ and strut has length } L$$

 Using the left end of the board as a reference for torque  $r_1 = r_T = L$  and  $r_S = \frac{L}{2}$ 

 conditions for static equilibrium are  $\sum F_x = 0$ ,  $\sum F_y = 0$ , and  $\sum \tau = 0$ 

$$\text{if } \sum \tau = 0 \text{ then } \tau_1 + \tau_S + \tau_T = 0 \text{ and } r_1 F_1 \sin \phi_1 + r_S F_S \sin \phi_S + r_T T \sin \phi_T = 0 \text{ so } T = \frac{-r_1 F_1 \sin \phi_1 - r_S F_S \sin \phi_S}{r_T \sin \phi_T}$$

$$T = \frac{-L(100 \text{ N}) \sin(-90^\circ) - \left(\frac{L}{2}\right)(100 \text{ N}) \sin(-90^\circ)}{L \sin 150^\circ} = \frac{-(100 \text{ N}) \sin(-90^\circ) - \left(\frac{1}{2}\right)(100 \text{ N}) \sin(-90^\circ)}{\sin 150^\circ} = \boxed{300 \text{ N}}$$

3.) (continued) looking at all the forces (and their components) acting on the strut

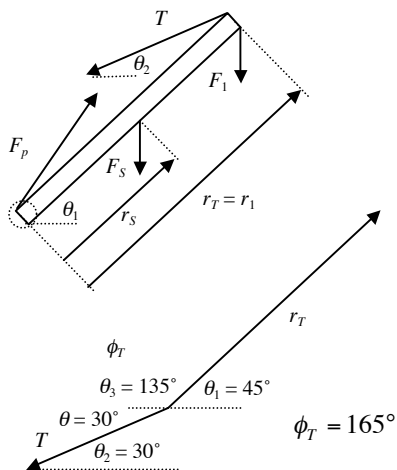


if  $\sum F_x = 0$  then  $F_{px} - T_x = 0$  and  $F_{px} = T_x = T \cos \theta_T = (300 \text{ N}) \cos 30^\circ = 260 \text{ N}$

if  $\sum F_y = 0$  then  $F_{py} + T_y - F_S - F_1 = 0$  and  $F_{py} = F_S + F_1 - T_y = 100 \text{ N} + 100 \text{ N} - (300 \text{ N}) \sin 30^\circ = 50 \text{ N}$

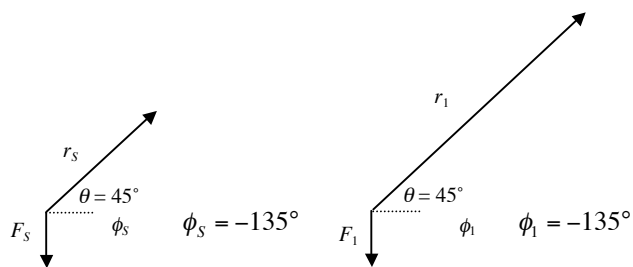
so  $F_p = \sqrt{F_{px}^2 + F_{py}^2} = \sqrt{(260 \text{ N})^2 + (50 \text{ N})^2} = \boxed{265 \text{ N}}$  and  $\theta_p = \tan^{-1} \frac{F_{py}}{F_{px}} = \tan^{-1} \left( \frac{50 \text{ N}}{260 \text{ N}} \right) = \boxed{10.9^\circ}$

4.)



$F_S = 100 \text{ N}$ ,  $F_1 = 100 \text{ N}$ ,  $\theta_1 = 45^\circ$ ,  $\theta_2 = 30^\circ$ , and strut has length  $L$

using the pivot point as a reference for torque  $r_T = r_1 = L$  and  $r_S = \frac{L}{2}$

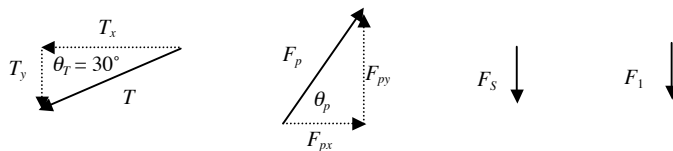


conditions for static equilibrium are  $\sum F_x = 0$ ,  $\sum F_y = 0$ , and  $\sum \tau = 0$

if  $\sum \tau = 0$  then  $\tau_1 + \tau_S + \tau_T = 0$  and  $r_1 F_1 \sin \phi_1 + r_S F_S \sin \phi_S + r_T T \sin \phi_T = 0$  so  $T = \frac{-r_1 F_1 \sin \phi_1 - r_S F_S \sin \phi_S}{r_T \sin \phi_T}$

$$T = \frac{-L(100 \text{ N}) \sin(-135^\circ) - \left(\frac{L}{2}\right)(100 \text{ N}) \sin(-135^\circ) - (100 \text{ N}) \sin(-135^\circ) - \left(\frac{1}{2}\right)(100 \text{ N}) \sin(-135^\circ)}{L \sin 165^\circ} = \frac{-100 \text{ N} \sin(-135^\circ) - \left(\frac{1}{2}\right)(100 \text{ N}) \sin(-135^\circ)}{\sin 165^\circ} = \boxed{410 \text{ N}}$$

looking at all the forces (and their components) acting on the strut

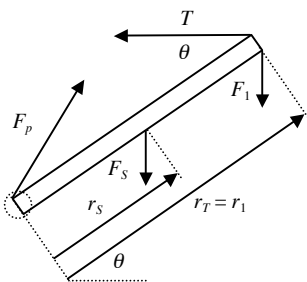


if  $\sum F_x = 0$  then  $F_{px} - T_x = 0$  and  $F_{px} = T_x = T \cos \theta_T = (410 \text{ N}) \cos 30^\circ = 355 \text{ N}$

if  $\sum F_y = 0$  then  $F_{py} - T_y - F_S - F_1 = 0$  and  $F_{py} = F_S + F_1 - T_y = 100 \text{ N} + 100 \text{ N} + (410 \text{ N}) \sin 30^\circ = 405 \text{ N}$

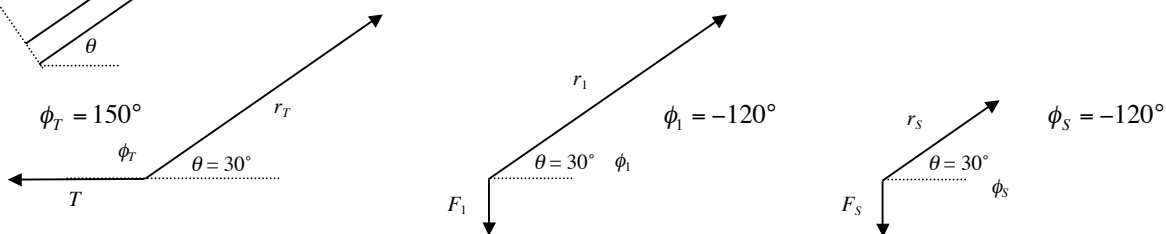
so  $F_p = \sqrt{F_{px}^2 + F_{py}^2} = \sqrt{(355 \text{ N})^2 + (405 \text{ N})^2} = \boxed{539 \text{ N}}$  and  $\theta_p = \tan^{-1} \frac{F_{py}}{F_{px}} = \tan^{-1} \left( \frac{405 \text{ N}}{355 \text{ N}} \right) = \boxed{48.8^\circ}$

5.)



$F_s = 100 \text{ N}$ ,  $F_1 = 100 \text{ N}$ ,  $\theta = 30^\circ$ , and strut has length  $L$

using the pivot point as a reference for torque  $r_T = r_1 = L$  and  $r_s = \frac{L}{2}$

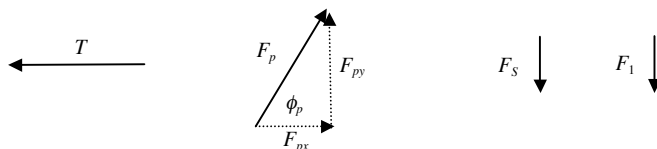


conditions for static equilibrium are  $\sum F_x = 0$ ,  $\sum F_y = 0$ , and  $\sum \tau = 0$

if  $\sum \tau = 0$  then  $\tau_1 + \tau_s + \tau_T = 0$  and  $r_1 F_1 \sin \phi_1 + r_s F_s \sin \phi_s + r_T T \sin \phi_T = 0$  so  $T = \frac{-r_1 F_1 \sin \phi_1 - r_s F_s \sin \phi_s}{r_T \sin \phi_T}$

$$T = \frac{-L(100 \text{ N})\sin(-120^\circ) - \left(\frac{L}{2}\right)(100 \text{ N})\sin(-120^\circ) - (100 \text{ N})\sin(-120^\circ) - \left(\frac{1}{2}\right)(100 \text{ N})\sin(-120^\circ)}{L\sin 150^\circ} = \frac{-100 \text{ N}\sin(-120^\circ) - \left(\frac{1}{2}\right)(100 \text{ N})\sin(-120^\circ)}{\sin 150^\circ} = \boxed{260 \text{ N}}$$

looking at all the forces (and their components) acting on the strut

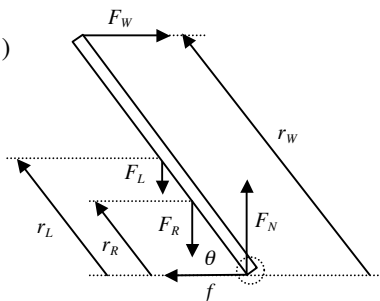


if  $\sum F_x = 0$  then  $F_{px} - T = 0$  and  $F_{px} = T = 260 \text{ N}$

if  $\sum F_y = 0$  then  $F_{py} - F_s - F_1 = 0$  and  $F_{py} = F_s + F_1 = 100 \text{ N} + 100 \text{ N} = 200 \text{ N}$

$$\text{so } F_p = \sqrt{F_{px}^2 + F_{py}^2} = \sqrt{(260 \text{ N})^2 + (200 \text{ N})^2} = \boxed{328 \text{ N}} \text{ and } \theta_p = \tan^{-1} \frac{F_{py}}{F_{px}} = \tan^{-1} \left( \frac{200 \text{ N}}{260 \text{ N}} \right) = \boxed{37.6^\circ}$$

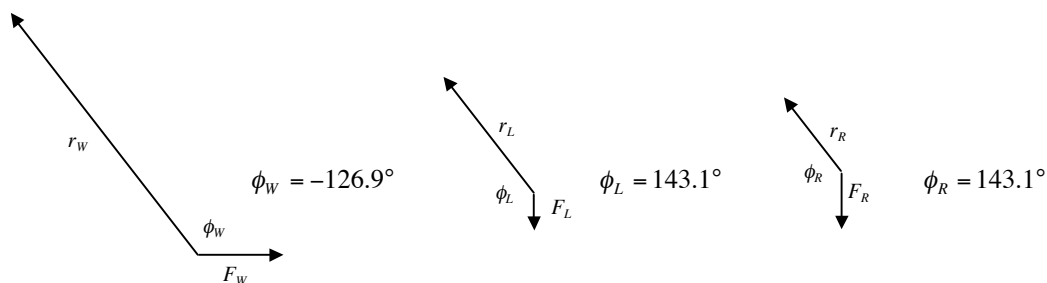
6.)



$F_L = 180 \text{ N}$ ,  $F_R = 800 \text{ N}$ ,  $\theta = 53.1^\circ$ , ladder is  $5.0 \text{ m}$  long

using the base of the ladder as a reference for torque

$r_W = 5.0 \text{ m}$ ,  $r_L = 2.5 \text{ m}$ , and  $r_R = \frac{5}{3} \text{ m}$



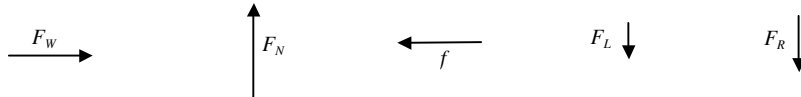
6.) (continued)

conditions for static equilibrium are  $\sum F_x = 0$ ,  $\sum F_y = 0$ , and  $\sum \tau = 0$

if  $\sum \tau = 0$  then  $\tau_W + \tau_L + \tau_R = 0$  and  $r_W F_W \sin \phi_W + r_L F_L \sin \phi_L + r_R F_R \sin \phi_R = 0$  so  $F_W = \frac{-r_L F_L \sin \phi_L - r_R F_R \sin \phi_R}{r_T \sin \phi_T}$

$$F_W = \frac{-(2.5 \text{ m})(180 \text{ N})\sin 143.1^\circ - \left(\frac{5}{3} \text{ m}\right)(800 \text{ N})\sin 143.1^\circ}{(5.0 \text{ m})\sin(-126.9^\circ)} = 268 \text{ N}$$

a.) looking at all forces acting on the ladder



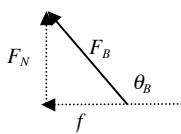
if  $\sum F_x = 0$  then  $F_W - f = 0$  and  $f = F_W = \boxed{268 \text{ N}}$

if  $\sum F_y = 0$  then  $F_N - F_L - F_R = 0$  and  $F_N = F_L + F_R = 180 \text{ N} + 800 \text{ N} = \boxed{980 \text{ N}}$

b.)

$$f = \mu F_N \text{ so } \mu = \frac{f}{F_N} = \frac{268 \text{ N}}{980 \text{ N}} = \boxed{0.27}$$

c.) the forces at the base are the frictional force  $f$  and the normal force  $F_N$  and they are orthogonal



$$F_B = \sqrt{f^2 + F_N^2} = \sqrt{(-268 \text{ N})^2 + (980 \text{ N})^2} = \boxed{1016 \text{ N}}$$

$$\theta_B = \tan^{-1} \frac{F_N}{f} = \tan^{-1} \left( \frac{980 \text{ N}}{-268 \text{ N}} \right) = -74.7^\circ + 180^\circ = \boxed{105.3^\circ}$$