

# Electricity and Circuits

## Charges in Motion

### Electric Current ( $I$ )

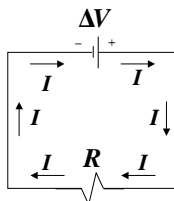
The net amount of charge that passes through a device per unit time at any point.

Current is defined as:

$$I = \frac{\Delta q}{\Delta t}$$

Electric current is measured in *coulombs per second* or *amperes*. ( $1 \text{ A} = 1 \text{ C/s}$ )

## Schematic Diagrams



The *direction of current* is by convention the *direction a positive charge moves* through the circuit, which is towards the negative terminal of the battery.

## Electric Circuits

An *electric circuit* is a *closed loop* around which charges flow.

A circuit consists of an energy source connected to a device that uses energy.

In a circuit, the charges that are moving are *electrons*.

## Batteries (*emf*)

In order to produce an electric current in a circuit, a potential difference is needed. Batteries are one way of providing a difference in potential (called *electromotive force* or *emf*). Potential difference is called voltage  $\Delta V$  and is measured in units of volts (V).

$$V [=] \frac{J}{C}$$



## Ohm's Law

Georg Ohm (1787-1854)

- Current depends upon the conductivity of the material.
- It is more common to talk about *resistance*  $R$  (inverse of conductivity) and express this relationship as:

$$I = \frac{\Delta V}{R} \text{ or } \Delta V = I \cdot R$$

- The unit for resistance is called the *ohm* and is abbreviated  $\Omega$  (omega)

## Voltage

Ohm's Law is often written as:

$$V_{ab} = I \cdot R$$

where:  $V_{ab} = V_a - V_b = \Delta V$

For power sources:



$$\Delta V = V_a - V_b = V_{ab} > 0$$

For resistive loads:



$$\Delta V_R = V_a - V_b = V_{ab} < 0$$

## Resistance ( $R$ ) and Resistivity ( $\rho$ )

It can be experimentally determined that the resistance of a wire is directly proportional to its length  $\ell$  and inversely proportional to its cross-sectional area  $A$ .

$$R = \frac{\rho \ell}{A}$$

The proportionality constant  $\rho$  is called the *resistivity* and depends upon the material used for the wire.

$$\rho [=] \Omega \cdot \text{m}$$

## Electric Power

*Power ( $P$ )* is the rate energy is transformed in a device.

$$P = I\Delta V$$

The unit for power is a J/s or watt ( $1 \text{ W} = 1 \text{ J/s}$ ).

For *resistors*, combining the above with Ohm's Law results in:

$$P = I^2 R = \frac{\Delta V^2}{R}$$

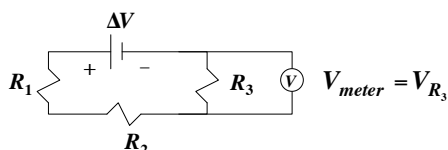
## Electric Energy

The total energy  $E$  (in joules) is the power in watts times the time in seconds.

$$E = Pt$$

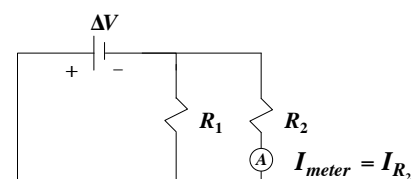
## Measuring Voltage

- *Voltmeters are placed in parallel* with the points between which the voltage measurement is made
- *Voltmeters have a very high resistance and do not affect the circuit* (they draw a very small current)

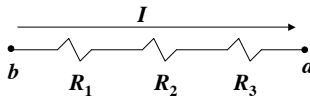


## Measuring Current

- *Ammeters are placed in series* with the device through which the current measurement is made
- *Ammeters have a very low resistance and do not affect the circuit* (the voltage drop is very low)



## Resistors in Series

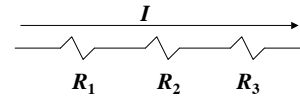


$$V_{ab} = \Delta V_1 + \Delta V_2 + \Delta V_3 = IR_1 + IR_2 + IR_3$$

$$V_{ab} = I(R_1 + R_2 + R_3)$$

$$I = \frac{V_{ab}}{R_1 + R_2 + R_3} = \frac{V_{ab}}{R_s}$$

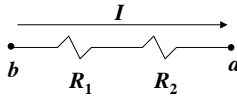
## Resistors in Series



- *Current is the same* through each resistor and is the same as the current in the equivalent resistance
- *Voltage drop across each resistor is different unless the resistance is the same.*

$$R_s = \sum_i R_i$$

## Resistors in Series (Voltage Divider)



$$I = \frac{V_{ab}}{R_1 + R_2}$$

$$\Delta V_1 = IR_1 = \frac{V_{ab}R_1}{R_1 + R_2}$$

$$\Delta V_2 = IR_2 = \frac{V_{ab}R_2}{R_1 + R_2}$$

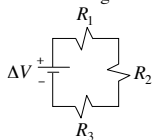
Example 3:

A 120  $\Omega$ , a 60  $\Omega$ , and a 40  $\Omega$  resistor are connected in series with a 110 V power source.

- Draw a schematic diagram.
- What is the equivalent resistance of the circuit?
- What is the current from the power source?
- What is the current through each resistor?
- What is the voltage drop across each resistor?

Example 3:  $R_1 = 120 \Omega$ ,  $R_2 = 60 \Omega$ ,  $R_3 = 40 \Omega$ , and  $\Delta V = 110 \text{ V}$

a.) schematic diagram in series



b.)  $R_{eq} = ?$

$$R_{eq} = R_1 + R_2 + R_3$$

$$R_{eq} = 120 \Omega + 60 \Omega + 40 \Omega$$

$$R_{eq} = 220 \Omega$$

c.)  $I = ?$

$$\Delta V = IR_{eq} \quad I = \frac{\Delta V}{R_{eq}} = \frac{110 \text{ V}}{220 \Omega} = 0.50 \text{ A}$$

d.)  $I$ 's = ? for each resistor

Resistors in series have the same current and the same current as their equivalent so:

$$I_1 = I_2 = I_3 = I = 0.50 \text{ A}$$

e.)  $\Delta V$ 's = ? for each resistor

$$\Delta V_1 = I_1 R_1$$

$$\Delta V_2 = I_2 R_2$$

$$\Delta V_3 = I_3 R_3$$

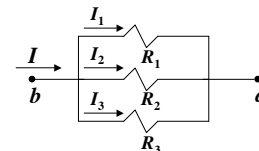
$$\Delta V_1 = (0.5 \text{ A})(120 \Omega) \quad \Delta V_2 = (0.5 \text{ A})(60 \Omega) \quad \Delta V_3 = (0.5 \text{ A})(40 \Omega)$$

$$\Delta V_1 = 60 \text{ V}$$

$$\Delta V_2 = 30 \text{ V}$$

$$\Delta V_3 = 20 \text{ V}$$

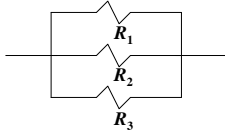
## Resistors in Parallel



$$I = I_1 + I_2 + I_3 = \frac{V_{ab}}{R_1} + \frac{V_{ab}}{R_2} + \frac{V_{ab}}{R_3} = \frac{V_{ab}}{R_p}$$

$$\frac{1}{R_p} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$$

## Resistors in Parallel



- *Voltage drop is the same* across each resistor and the same as the voltage drop across the equivalent resistance
- Current is different through each resistor, the higher the resistance the lower the current

$$\frac{1}{R_p} = \sum_i \frac{1}{R_i}$$

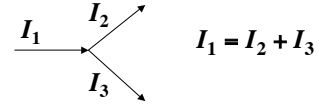
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## Kirchhoff's Rules

### 1.) *Junction Rule* (Conservation of charge)

At any junction point, the sum of all currents entering the junction must equal the sum of all currents leaving the junction.



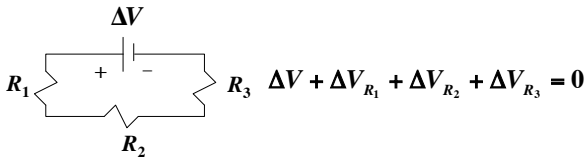
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## Kirchhoff's Rules

### 2.) *Loop Rule* (Conservation of energy)

The sum of the changes in potential around any closed path of a circuit is zero.



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